

Math III Unit 3 Review

SHOW ALL WORK FOR FULL CREDIT!!!

Name: _____ Key

For number 1, (a) Simplify and write in standard form and classify by (b) degree and (c) number of terms.

(NC.M3.A-SSE.2 DOK 2)

$$1. (-2x^4) - x^2 + 8 + (3x^4) - 2x - 5$$

Combine like terms

$$1a. x^4 - x^2 - 2x + 3$$

1b. Quartic

1c. polynomial

2. Find the zeros of $y = 3x(x - 9)(x + 4)$

$$\begin{array}{l} 3x = 0 \\ \hline x = 0 \end{array} \quad \begin{array}{l} x - 9 = 0 \\ \hline x = 9 \end{array} \quad \begin{array}{l} x + 4 = 0 \\ \hline x = -4 \end{array}$$

$$2. x = 0, 9, -4$$

For question 3 (1) find the zeros of the function, (2) simplify and write in standard form and (3) classify using the degree and # of terms. (NC.M3.A-APR.3 DOK 2)

$$3. f(x) = (x + 1)(x - 2)^2$$

$$\begin{array}{lll} x + 1 = 0 & (x - 2)(x - 2) = 0 \\ x = -1 & x = 2 & x = 2 \end{array}$$

$$\begin{array}{l} (x+1)(x-2)(x-2) \\ (x+1)(x^2 - 4x + 4) \end{array}$$

$$\begin{array}{|c|c|c|c|} \hline x^2 & -4x & 4 \\ \hline x^3 & -4x^2 & 4x \\ \hline 1 & x^2 & -4x & 4 \\ \hline \end{array}$$

$$\text{Zeros: } x = -1, 2, 2$$

$$\text{Standard form: } x^3 - 3x^2 + 4$$

Classify-Degree: Cubic

Classify-# of term(s): Trinomial

Factor the following for #4-5. Show ALL work. (NC.M3.A-APR.3 DOK 1)

$$B. 4. x^3 - 7x^2 - 8x$$

$$x(x^2 - 7x - 8)$$

- a) $(2x - 1)(x + 4)$
- b) $x(x + 1)(x - 8)$
- c) $x(2x - 1)(x + 4)$
- d) $(x + 1)(x - 8)$

$$D. 5. 3x^2 - 60x + 300$$

$$3(x^2 - 20x + 100)$$

- a) $(x + 10)(x - 10)$
- b) $3(x + 10)(x - 10)$
- c) $(x + 30)(x - 30)$
- d) $3(x - 10)^2$

~~$$\begin{array}{r} 100 \\ -10 \\ \hline -10 \\ -20 \\ \hline \end{array}$$~~

Solve by factoring for #6-7. Show ALL work and give exact answers. (NC.M3.A-APR.3 DOK 1)

$$6. x^4 - 8x^2 = 48$$

$$x^4 - 8x^2 - 48 = 0$$

$$(x^2 - 12)(x^2 + 4) = 0$$

$$x^2 - 12 = 0$$

$$x^2 = 12$$

$$x = \pm 2\sqrt{3}$$

$$x^2 + 4 = 0$$

$$x^2 = -4$$

$$x = \pm 2i$$

$$7. x^3 - 2x^2 + 9x - 18 = 0$$

$$\begin{array}{|c|c|c|c|} \hline x^2 & x^3 & -2x^2 & \\ \hline 9 & 9x & -18 & \\ \hline \end{array}$$

$$(x^2 + 9)(x - 2) = 0$$

$$\begin{array}{r} x^2 = -9 \\ x = \pm 3i \end{array}$$

$$x = 2$$

8. Factor $x^2 - y^2$

$$(x+y)(x-y)$$

Graph

in your TI-84

9. Determine which binomial is a factor of: $x^3 - x^2 + 4x - 12$.

[2nd] trace
#2

a) $(x+2)$

b) $(x+8)$

c) $(x-2)$

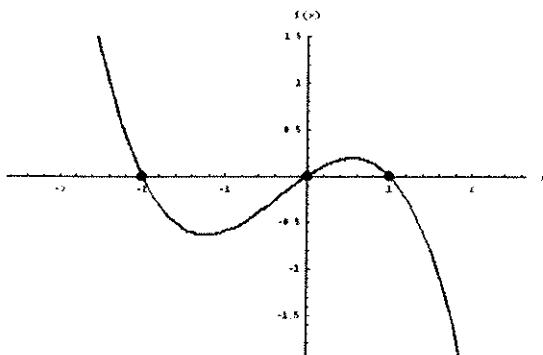
d) $(x-8)$

$x=2$

-2 -2

$(x-2) = 0$

10. What are the zeros of the following graph? (NC.M3.A-APR.3 DOK 1)



10. $x = -2, 0, 1$

11. Solve by completing the square: $x^2 - 6x + 41 = 0$. (NC.M3.A-APR.3 DOK 3)

$$x^2 - 6x + \boxed{9} = -41 + \boxed{9}$$

$$\sqrt{(x-3)^2} = \sqrt{-32}$$

~~32~~
~~16~~ . 2

$$x-3 = \pm 4\sqrt{2}i$$

$$\boxed{x = 3 \pm 4\sqrt{2}i}$$

Step 1: Factor out GCF

Step 2: Add or Subtract the "C" part to the right side

Step 3: Complete the sq.

Step 4: Simplify & Square it both sides

Step 5: Solve for x

12. Write the polynomial in standard form that has zeros of $0, -\frac{2}{3}$, and 2 . (NC.M3.F-BF.1a DOK 2)

$$x = 0$$

$$x = -\frac{2}{3}$$

$$x = 2$$

$$3x = -2$$

$$(x-2) = 0$$

$$(3x+2) = 0$$

$$x(3x+2)(x-2)$$

$$x(3x^2 - 4x - 4)$$

$$\boxed{3x^3 - 4x^2 - 4x}$$

$x - 2$	
$3x$	$3x^2 - 6x$
2	$2x - 4$

Write the polynomial in standard form that has zeros of 2 and $-4i$. (NC.M3.F-BF.1b DOK 2)

$$x = 2$$

$$(x-2) = 0$$

$$x = \pm 4i$$

$$(x)^2 = (\pm 4i)^2$$

$$x^2 = -16$$

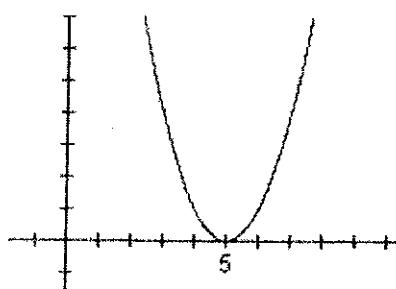
$$(x^2 + 16) = 0$$

$$(x-2)(x^2+16)$$

i 's and \sqrt{i} 's come in conjugate pairs!

$x^3 - 2x^2 + 16x - 32$	x^2	16
x	x^3	16x
-2	$-2x^2$	-32

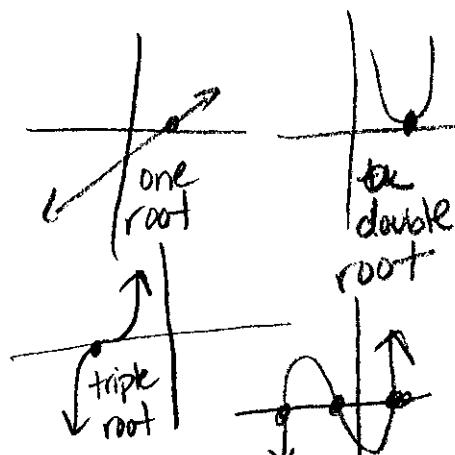
14. Write the polynomial in standard form given the graph. (NC.M3.F-BF.1a DOK 2)



$$(x-5)^2 \text{ bounce}$$

$$(x-5)(x-5)$$

$$x^2 - 10x + 25$$



Divide using synthetic or long division. (NC.M3.A-APR.2 DOK 1)

15. $(50x^3 + 10x^2 - 35x - 7) \div (5x - 4)$

$$\begin{array}{r} 10x^2 + 10x + 1 \\ 5x - 4 \overline{)50x^3 + 10x^2 - 35x - 7} \\ - (50x^3 - 40x^2) \quad \downarrow \\ \hline (50x^2 - 35x) \quad \downarrow \\ - (50x^2 - 40x) \quad \downarrow \\ \hline (5x) - 7 \quad \downarrow \\ - (5x - 4) \quad \downarrow \\ \hline - 3 \end{array}$$

15. $10x^2 + 10x + 1 - \frac{3}{5x-4}$

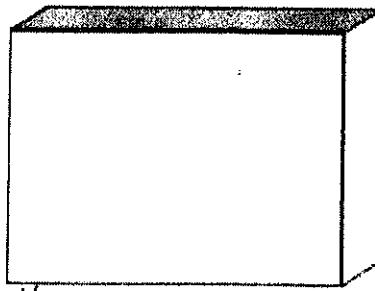
16. $\frac{x^3 - 13x^2 + 40x + 18}{x-7}$

$$\begin{array}{r} 1 -13 40 18 \\ \downarrow 7 -42 -14 \\ 1 -6 -2 4 \end{array}$$

not a triple root it's (3)
individual roots

16. $x^2 - 6x - 2 + \frac{4}{x-7}$

17. The dimensions of this rectangular prism are given algebraically. Write a polynomial function that represents the **volume** of this prism in **standard** form. (NC.M3.G-GMD.3 DOK 3)



$$x+2$$

$$x-4$$

$$x+1$$

$$(x+2)(x-4)(x+1)$$

$$(x+2)(x^2 - 3x - 4)$$

$$V(x) = \underline{x^3 - x^2 - 10x - 8}$$

	x^2	$-3x$	-4
x	x^3	$-3x^2$	$-4x$
z	$2x^2$	$-6x$	-8

$$V = l \times w \times h$$

18. A rectangle has the dimensions of $(x - 2)$ and $(-x + 10)$. (NC.M3.A-SSE.1a DOK 3)

a) Write an equation to model the area in factored form of the rectangle.

$$f(x) = (x-2)(-x+10)$$

$$A = l \times w$$

b) At what x-value does the maximum area occur? 2nd PACE #4

$$x = 6$$

c) What is the maximum area of the box?

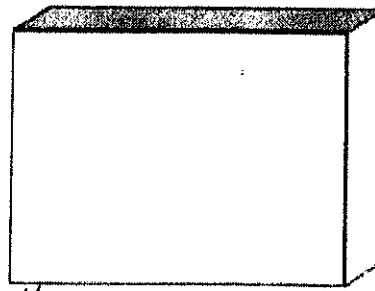
maximum area of the box is 16.

17. The dimensions of this rectangular prism are given algebraically. Write a polynomial function that represents the volume of this prism in **standard** form. (NC.M3.G-GMD.3 DOK 3)

$$(x+2)(x-4)(x+1)$$

$$(x+2)(x^2 - 3x - 4)$$

$$V(x) = \underline{x^3 - x^2 - 10x - 8}$$



x + 2

x - 4

x + 1

	x^2	-3x	-4
X	x^3	$-3x^2$	$-4x$
Z	$2x^2$	$-6x$	-8

$$V = l \times w \times h$$

18. A rectangle has the dimensions of $(x - 2)$ and $(-x + 10)$. (NC.M3.A-SSE.1a DOK 3)

a) Write an equation to model the area in factored form of the rectangle.

$$f(x) = (x-2)(-x+10)$$

$$A = l \times w$$

b) At what x-value does the maximum area occur? 2nd PACE #4

$$x = 6$$

c) What is the maximum area of the box?

maximum area of the box is 16.